



DiffRGD: An Inference-Time Diffusion Guidance Through Riemannian Gradient Descent



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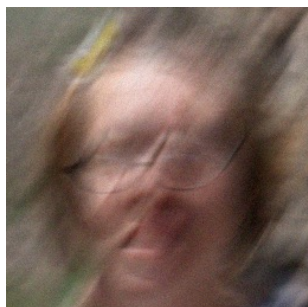


Inference-Time Diffusion Controlling

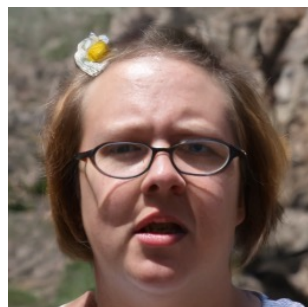
Image Inverse Problem

$$\mathbf{y} = \mathcal{A}\mathbf{x} + \boldsymbol{\eta}$$

Operator Noise



Measurement $\mathbf{y}$

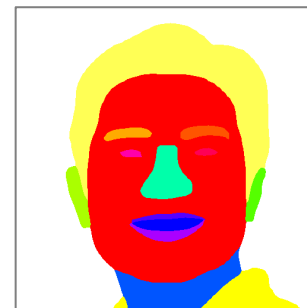


Reconstruction $\hat{\mathbf{x}}$

$$\mathcal{L}_{\text{IP}}(\mathbf{x}, \mathbf{y}) = \|\mathcal{A}\mathbf{x} - \mathbf{y}\|_2^2$$

Conditional Generation (Segmentation Mask)

ψ : Face Segmentation Model



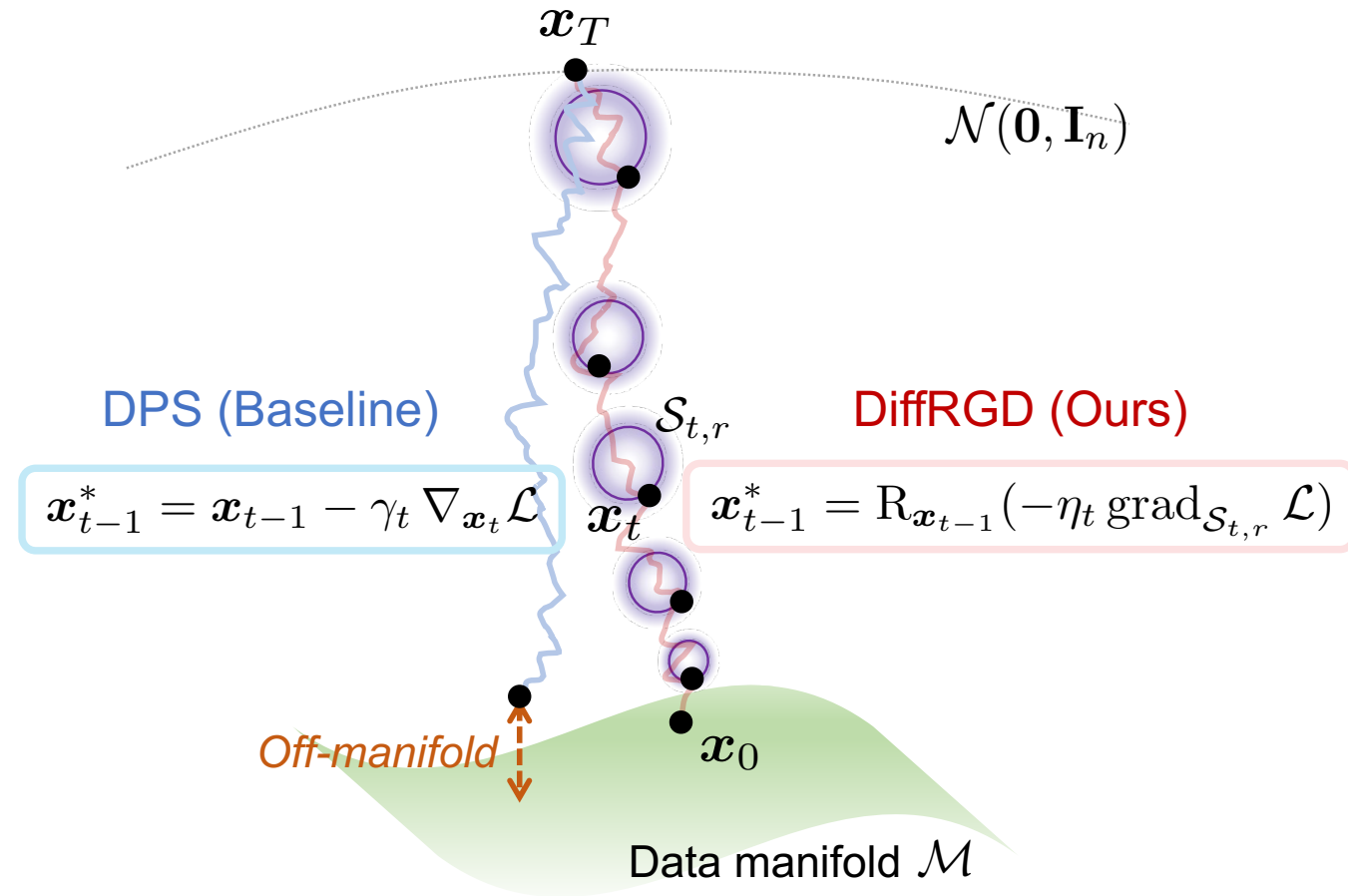
Condition $\mathbf{y}$



Generation $\hat{\mathbf{x}}$

$$\mathcal{L}_{\text{Seg}}(\mathbf{x}, \mathbf{y}) = \|\psi(\mathbf{x}) - \mathbf{y}\|_2^2$$

Distribution Preserving Diffusion Guidance



Research Question: *Can we design latent-distribution-aware guidance that ensures the guided sample lies within the original latent distribution?*

Distribution-induced Geometry

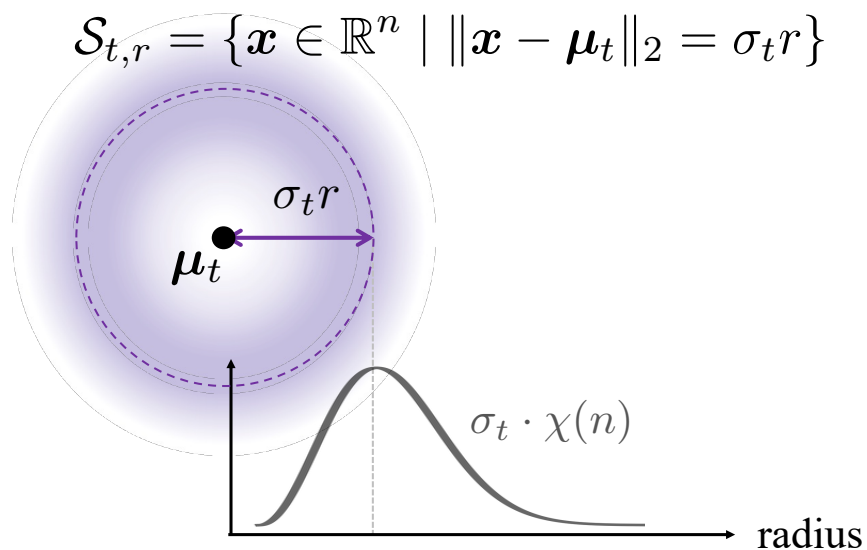
Constructing the geometric structure

Polar Decomposition of Isotropy Gaussian

$$\mathbf{x}_{t-1} \sim \mathcal{N}(\boldsymbol{\mu}_t, \sigma_t^2 \mathbf{I}_n) \iff \mathbf{x}_{t-1} = \boldsymbol{\mu}_t + \sigma_t r \mathbf{u}$$

$$r \sim \chi(n)$$

$$\mathbf{u} \sim \text{Unif}(\mathbb{S}^{n-1})$$



Constraint Optimization

$$\mathbf{x}_{t-1} = \operatorname{argmin}_{\mathbf{x} \in \mathcal{S}_{t,r}} \mathcal{L}(\hat{\mathbf{x}}_0(\mathbf{x}, t-1), \mathbf{y})$$

Diffusion Guidance with Riemannian Gradient Descent

Tangent Space

$$T_x \mathcal{S}_{t,r} := \{v \in \mathbb{R}^n \mid (x - \mu_t)^\top v = 0\}$$

Projection Operator

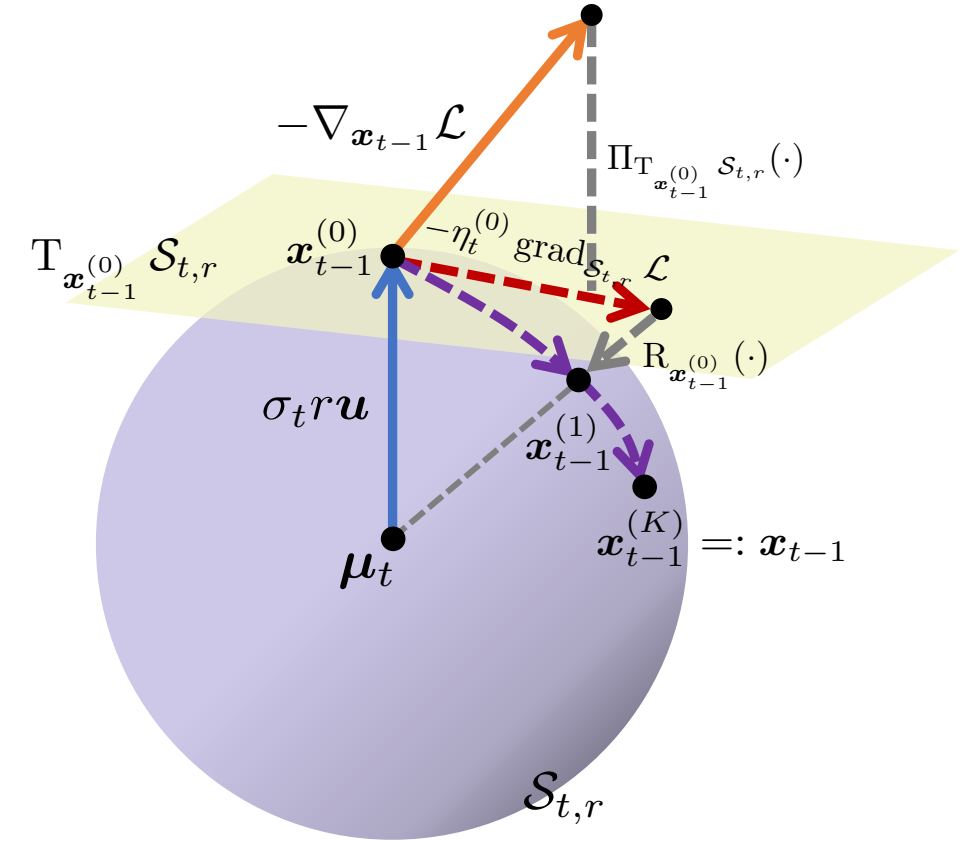
$$\Pi_{T_x \mathcal{S}_{t,r}}(v) := \left(\mathbf{I}_n - \frac{(x - \mu_t)(x - \mu_t)^\top}{\|x - \mu_t\|_2^2} \right) v$$

Retraction

$$R_x(v) := \mu_t + \sigma_t r \cdot \frac{x - \mu_t + v}{\|x - \mu_t + v\|_2}$$

Riemannian Gradient

$$\text{grad}_{\mathcal{S}_{t,r}} \mathcal{L} := \Pi_{T_{x_{t-1}^{(k)}} \mathcal{S}_{t,r}} \left(\nabla_{x_{t-1}^{(k)}} \mathcal{L}(\hat{x}_0(x_{t-1}^{(k)}, t-1), y) \right)$$

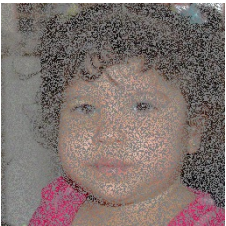
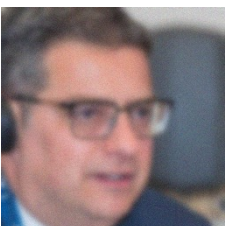
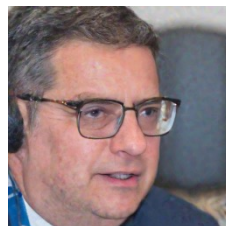
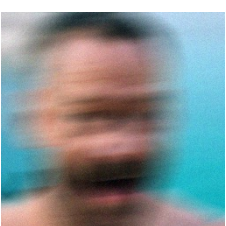
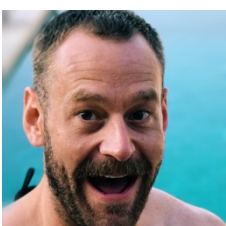
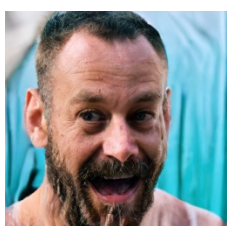
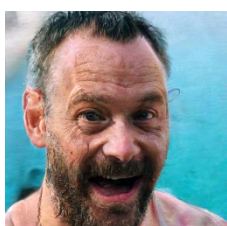
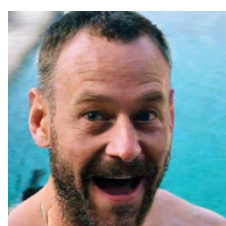
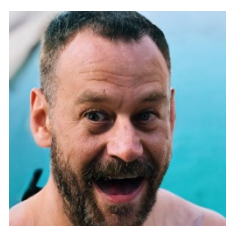
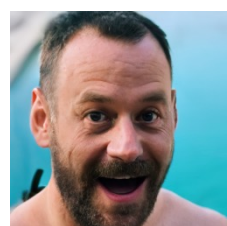


$$x_{t-1}^{(k+1)} = R_{x_{t-1}^{(k)}} \left(-\eta_t^{(k)} \text{grad}_{\mathcal{S}_{t,r}} \mathcal{L} \right)$$

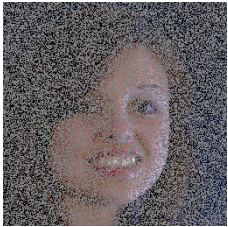
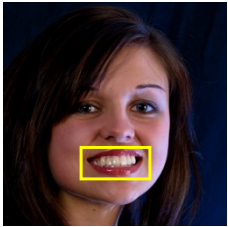
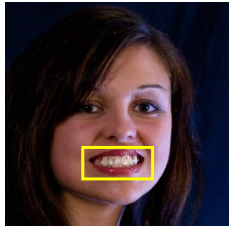
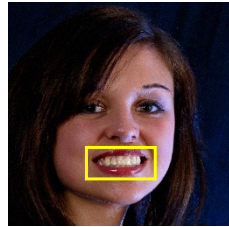
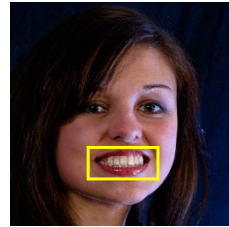
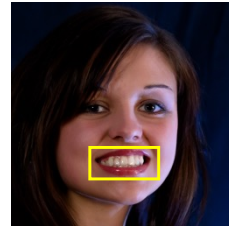
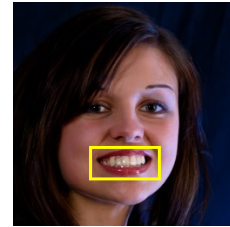
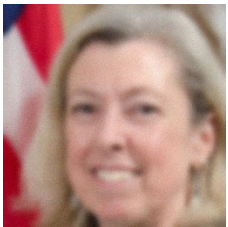
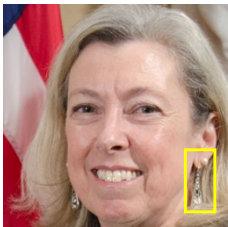
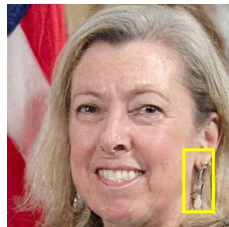
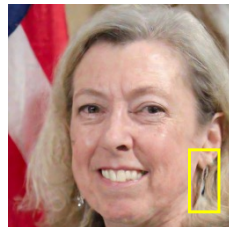
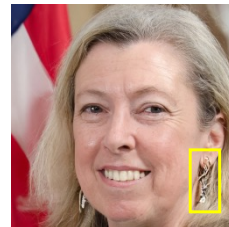
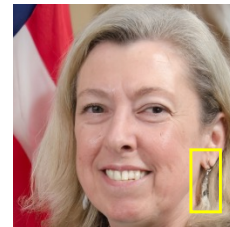
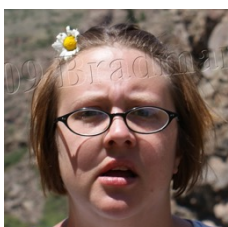
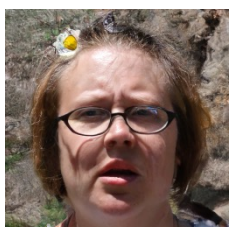
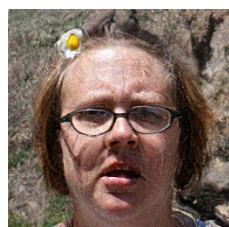
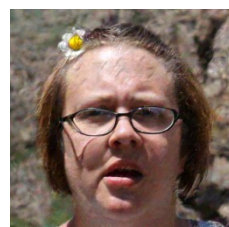
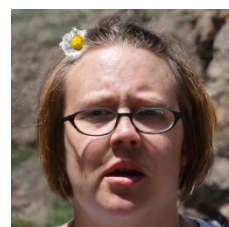
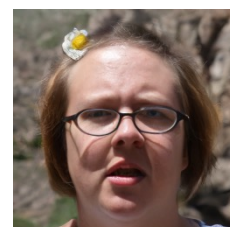
Experiments: Image Inverse Problems

Tasks	Methods	Venue	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	FID $\downarrow$
Inpainting	DPS [5]	ICLR 2023	30.44	0.863	0.153	42.68
	MPGD [13]	ICLR 2024	27.51	0.724	0.256	68.24
	DSG [51]	ICML 2024	31.03	0.866	0.144	36.30
	ADMMDiff [56]	CVPR 2025	<u>32.38</u>	<u>0.899</u>	<u>0.119</u>	<u>29.52</u>
	DiffRGD (Ours)	-	34.04*	0.926*	0.096*	21.88*
Super-Resolution 4 $\times$	DPS [5]	ICLR 2023	26.03	0.727	0.260	80.05
	MPGD [13]	ICLR 2024	24.40	0.614	0.354	101.50
	DSG [51]	ICML 2024	<u>26.71</u>	<u>0.737</u>	<u>0.256</u>	<u>74.67</u>
	ADMMDiff [56]	CVPR 2025	26.48	0.712	0.297	96.69
	DiffRGD (Ours)	-	27.77*	0.783*	0.220*	63.94*
Gaussian Deblurring	DPS [5]	ICLR 2023	25.88	0.721	0.237	69.38
	MPGD [13]	ICLR 2024	24.07	0.576	0.328	95.12
	DSG [51]	ICML 2024	27.45	0.751	0.259	<u>75.85</u>
	ADMMDiff [56]	CVPR 2025	26.57	0.757	<u>0.226</u>	79.30
	DiffRGD (Ours)	-	<u>26.80</u>	0.757	0.218*	63.83*
Motion Deblurring	DPS [5]	ICLR 2023	24.47	0.685	0.271	80.75
	MPGD [13]	ICLR 2024	23.15	0.569	0.357	106.99
	DSG [51]	ICML 2024	<u>26.80</u>	0.709	0.290	87.96
	ADMMDiff [56]	CVPR 2025	27.26	0.778	0.222	72.92
	DiffRGD (Ours)	-	25.84	<u>0.736</u>	<u>0.250</u>	72.26

Experiments: Image Inverse Problems

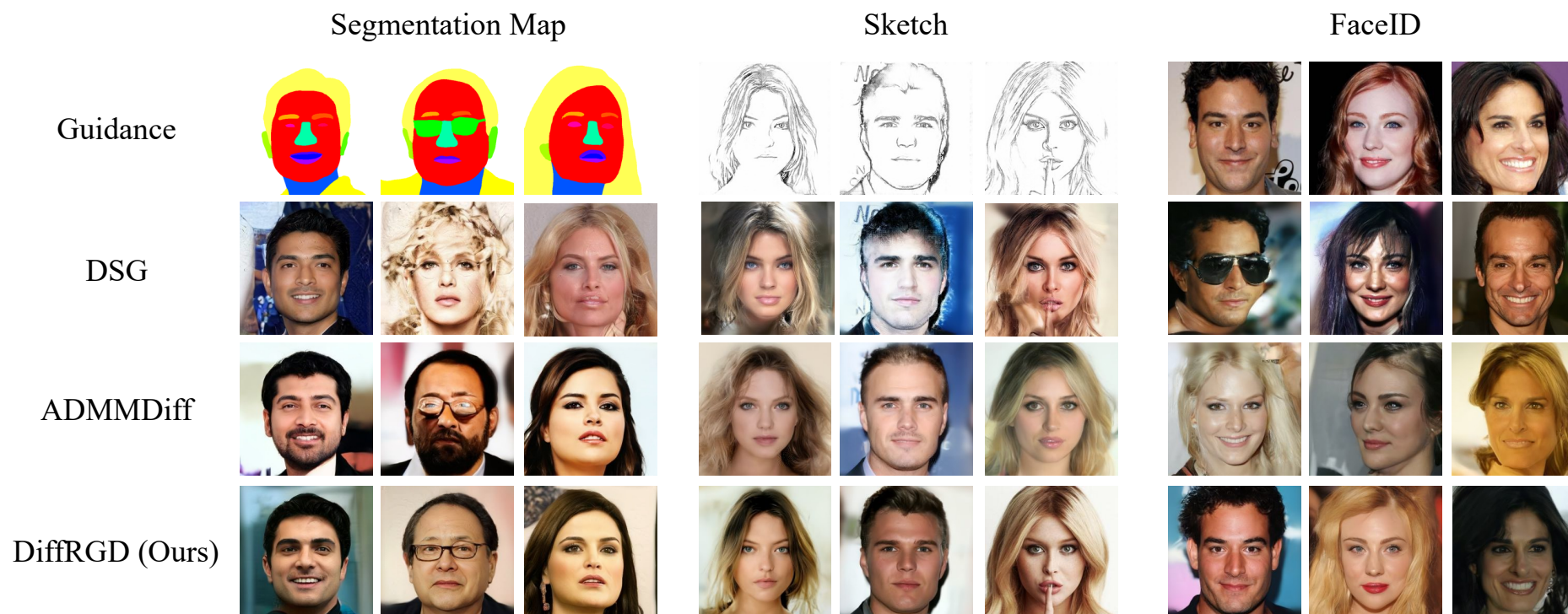
	Measurement	Ground Truth	DPS	MPGD	DSG	ADMMDiff	DiffRGD (Ours)
Inpainting							
Super-Resolution							
Gaussian Deblurring							
Motion Deblurring							

Experiments: Image Inverse Problems

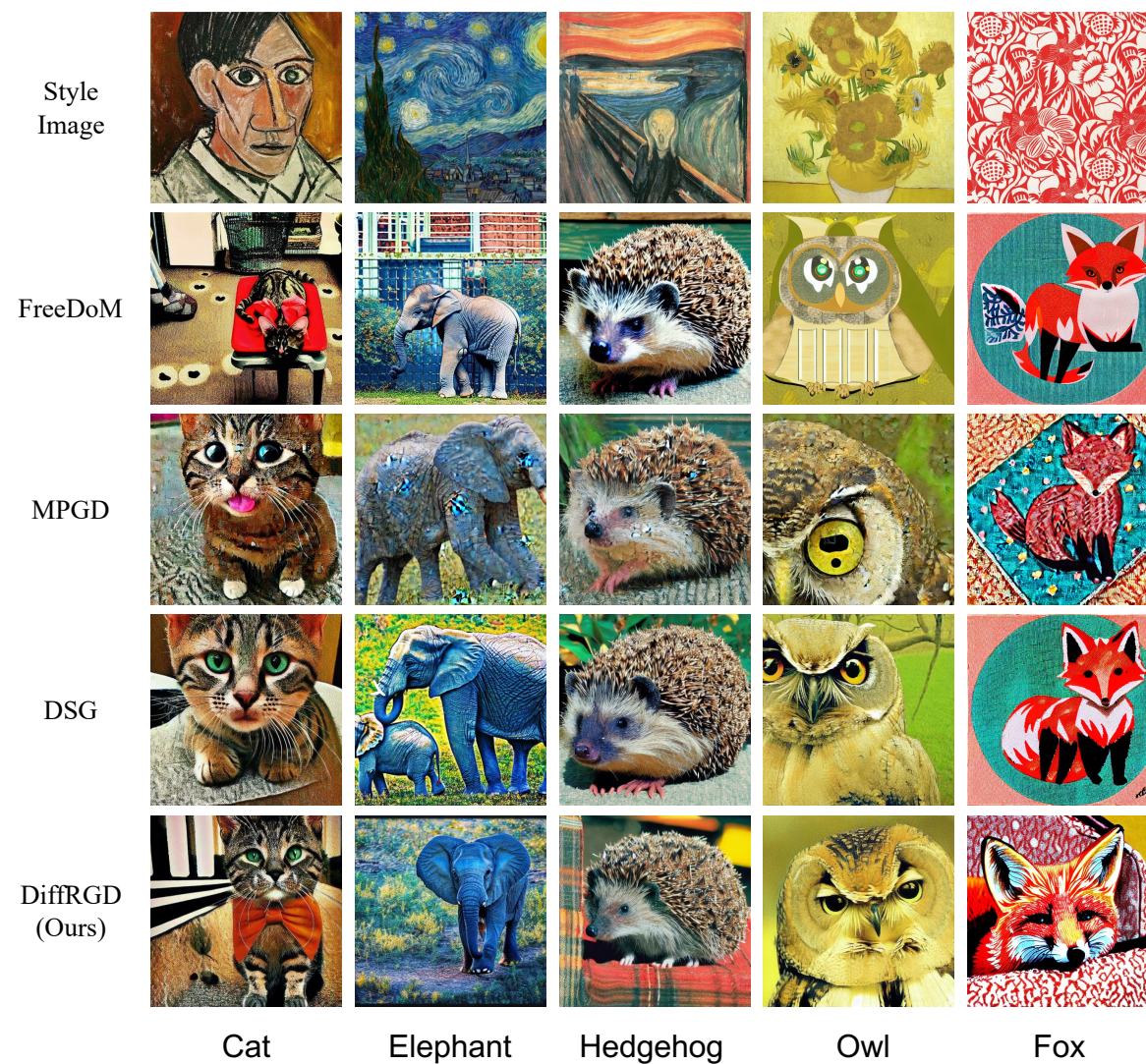
	Measurement	Ground Truth	DPS	MPGD	DSG	ADMMDiff	DiffRGD (Ours)
Inpainting							
Super-Resolution							
Gaussian Deblurring							
Motion Deblurring							

Experiments: Conditional Generation

Methods	Segmentation Map			Sketch			FaceID		
	mIoU $\uparrow$	FID $\downarrow$	KID $\downarrow$	Sketch- ℓ_2 $\downarrow$	FID $\downarrow$	KID $\downarrow$	FaceID- ℓ_2 $\downarrow$	FID $\downarrow$	KID $\downarrow$
FreeDoM [53]	0.622	156.02	0.057	30.85	101.90	0.017	0.557	127.05	0.032
DSG [51]	0.750	117.48	<u>0.028</u>	<u>21.36</u>	107.00	0.024	<u>0.340</u>	<u>95.27</u>	<u>0.014</u>
ADMMDiff [56]	<u>0.758</u>	<u>101.86</u>	0.031	30.82	<u>97.52</u>	<u>0.014</u>	0.346	100.81	<u>0.014</u>
DiffRGD (Ours)	0.804*	96.10*	0.026	19.48*	87.82*	0.012	0.303*	93.80	0.011



Experiments: Style-Guided Generation



Takeaways

- Respecting the latent Gaussian geometry is crucial for effective inference-time diffusion guidance. Diffusion guidance should preserve the data distribution.
- DiffRGD performs guidance on a distribution-induced spherical manifold using Riemannian Gradient Descent, preserving distributional fidelity while enabling effective control.
- DiffRGD is training-free and plug-and-play, achieving strong performance across diverse image restoration and conditional generation tasks.

Thank you!